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“Lipschitz-free spaces over Cantor sets and approximation properties”

Let $K = 2^{\mathbb{N}}$ be the Cantor set, let \mathcal{M} be the set of all metrics d on K that give its usual (product) topology, and equip \mathcal{M} with the topology of uniform convergence, where the metrics are regarded as functions on K^2 . In this talk we show that the set of metrics $d \in \mathcal{M}$ for which the Lipschitz-free space $\mathcal{F}(K, d)$ has the metric approximation property is a residual $F_{\sigma\delta}$ set in \mathcal{M} , and that the set of metrics $d \in \mathcal{M}$ for which $\mathcal{F}(K, d)$ fails the approximation property is a dense meager set in \mathcal{M} . This answers a question by G. Godefroy.
